

Relationship and inbreeding coefficients

Relationship coefficient $R_{xy} = \frac{\left(\frac{1}{2}\right)^{n+n'} (1 + F_{CA})}{\sqrt{(1 + F_X)(1 + F_Y)}}$

Inbreeding coefficient $F_X = \left(\frac{1}{2}\right)^{ns + nd + 1} (1 + F_{CA})$

Computing relationship and inbreeding using path coefficients

- **Wright** is responsible for the idea of tracing paths to establish the relationships among animals.

Step1: Convert the **bracket** pedigree to an **arrow** diagram in which each individual appears only **once**.

Step2: Locate **common ancestors (CA)**

For inbreeding coefficients: common ancestors are defined to be common to both the **sire** and the **dam** of inbred individuals (**X**).

For relationship coefficients: common ancestors are defined to be common to the **two individuals** of interest (**x** and **y**)

Relationship and inbreeding coefficients

Step 3: calculate the **inbreeding** coefficient for **inbred common** ancestors

Step 4: Full in the following table

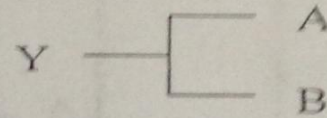
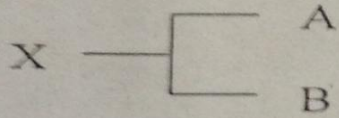
Common ancestor	Paths	$(1/2)^{n+n_1}$ for R_{xy} or $(1/2)^{ns+nd+1}$ for F_x	1+FCA	Product of lost two columns

Step 5: Sum the last column to compute the numerator of R_{xy} or F_x

Step 6: R_{xy} calculations only: divided the sum by $\sqrt{1+F_x} \sqrt{1+F_y}$

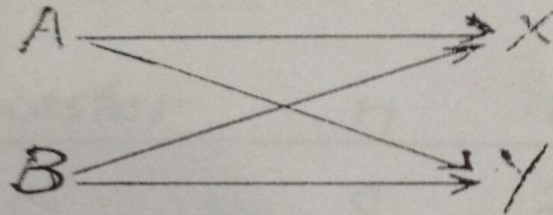
Relationship and inbreeding coefficients

1. From the following bracket pedigree:



Compute R_{XY}

Solution:



R_{XY}

ancestor	n	n'	$(1 + F_a)$	
A	1	1	—	$= (\frac{1}{2})^2$
B	1	1	—	$= (\frac{1}{2})^2$

$$R_{XY} = (\frac{1}{2})^2 + (\frac{1}{2})^2$$
$$= 0.25 + 0.25$$

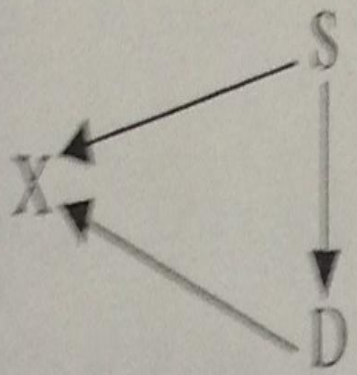
$$= 0.50$$

= 50% — Full sib.

Relationship and inbreeding coefficients

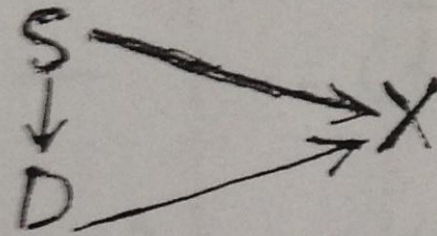
4. Calculate the inbreeding coefficient of individual X (F_X) and the relationship coefficient of the sire and dam (R_{SD}) in the following arrow diagrams of pedigrees.

(A)



Relationship and inbreeding coefficients

Solution:



(A)

$$F_X = \frac{\text{ancestors } n_S \quad n_D \quad 1 \quad (1+F_D)}{S \quad 0 \quad 1 \quad 1 \quad -} = \left(\frac{1}{2}\right)^2$$

$$F_X = \left(\frac{1}{2}\right)^2 = 0.25$$

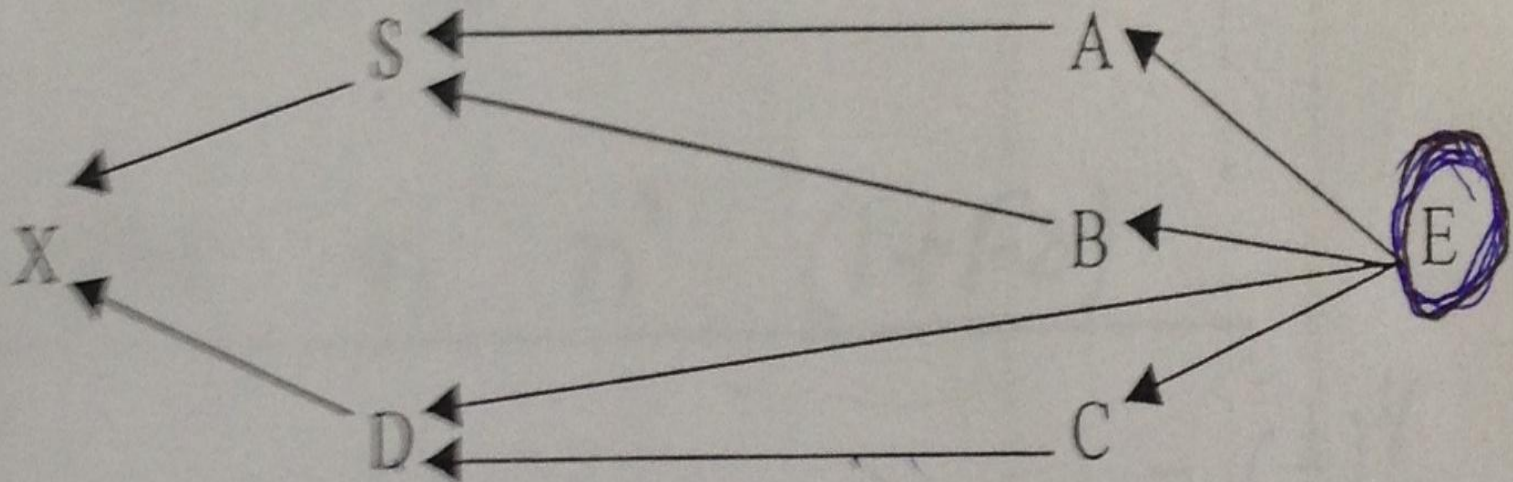
$$R_{SD} = \frac{\text{ancestors } n \quad \hat{n} \quad (1+F_D)}{S \quad 0 \quad 1 \quad -} = \left(\frac{1}{2}\right)^1$$

$$R_{SD} = \left(\frac{1}{2}\right)^1 = 0.50$$

Relationship and inbreeding coefficients

4. Calculate the inbreeding coefficient of individual X (F_X) and the relationship coefficient of the sire and dam (R_{SD}) in the following arrow diagrams of pedigrees.

(B)

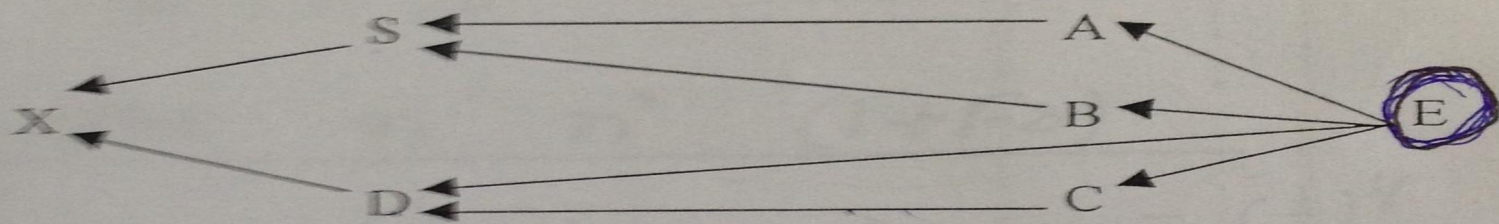


Also calculate R_{XE} for this pedigree.

F_X, R_{XE}

Relationship and inbreeding coefficients

(B)



Also calculate R_{XE} for this pedigree.

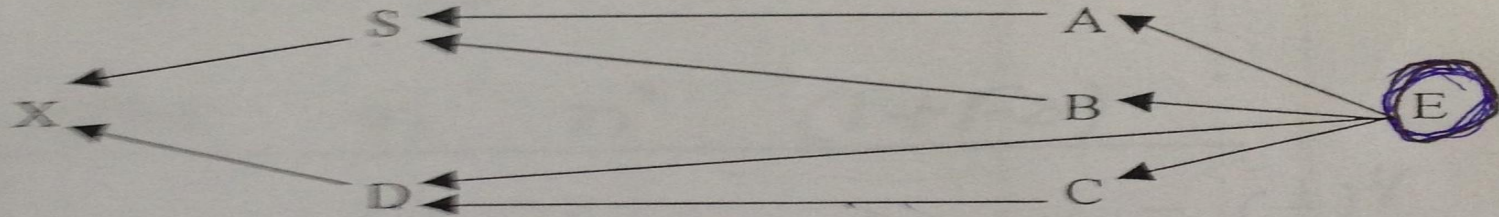
F_X, R_{XE}

F_X	ancestor	ns	nd	1	$(1 + Fa)$	
	E	2	2	1	—	$= (\frac{1}{2})^5$
	E	2	1	1	—	$= (\frac{1}{2})^4$
	E	2	2	1	—	$= (\frac{1}{2})^5$
	E	2	1	1	—	$= (\frac{1}{2})^4$

$$\begin{aligned}
 F_X &= (\frac{1}{2})^5 + (\frac{1}{2})^4 + (\frac{1}{2})^5 + (\frac{1}{2})^4 \\
 &= 0.03125 + 0.0625 + 0.03125 + 0.0625 \\
 &= 0.1875 \\
 &= 18.75\%
 \end{aligned}$$

Relationship and inbreeding coefficients

(B)



Also calculate R_{XE} for this pedigree.

F_X, R_{XE}

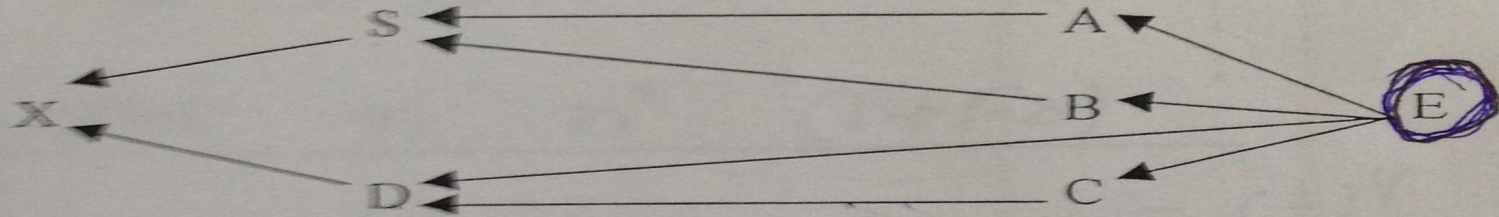
R_{SD}

ancestor	n	n'	$(1+F_a)$	
E	2	2	—	$= (\frac{1}{2})^4$
E	2	1	—	$= (\frac{1}{2})^3$
E	2	1	—	$= (\frac{1}{2})^3$
E	2	2	—	$= (\frac{1}{2})^4$

$$\begin{aligned}
 R_{SD} &= (\frac{1}{2})^4 + (\frac{1}{2})^3 + (\frac{1}{2})^3 + (\frac{1}{2})^4 \\
 &= 0.0625 + 0.125 + 0.125 + 0.0625 \\
 &= 0.375
 \end{aligned}$$

Relationship and inbreeding coefficients

(B)



Also calculate R_{XE} for this pedigree.

F_X, R_{XE}

$$F_S = \frac{\text{ancestor} \quad n_s \quad n_d \quad 1 \quad (1+F_0)}{E \quad 1 \quad 1 \quad 1 \quad - = \left(\frac{1}{2}\right)^3}$$

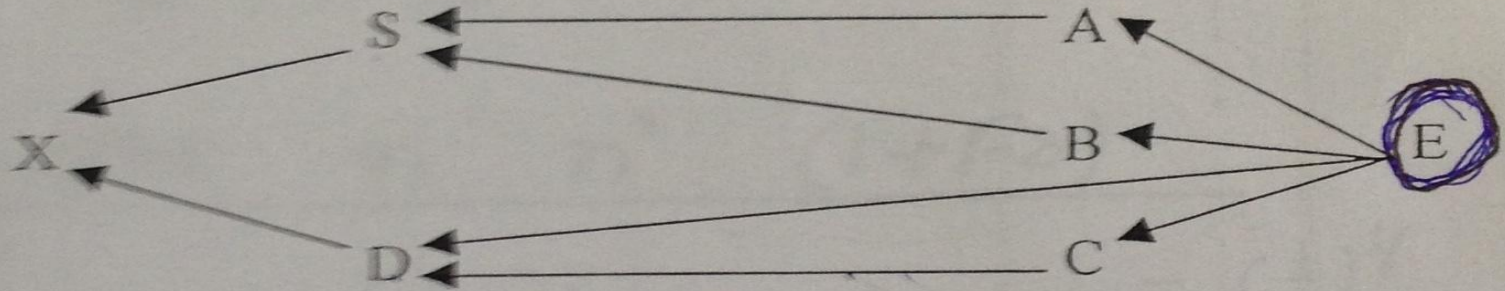
$$F_S = \left(\frac{1}{2}\right)^3 = 0.125$$

$$F_D = \frac{\text{ancestor} \quad n_s \quad n_d \quad 1 \quad (1+F_0)}{E \quad 0 \quad 1 \quad 1 \quad - = \left(\frac{1}{2}\right)^2}$$

$$F_S = \left(\frac{1}{2}\right)^2 = 0.25$$

Relationship and inbreeding coefficients

(B)



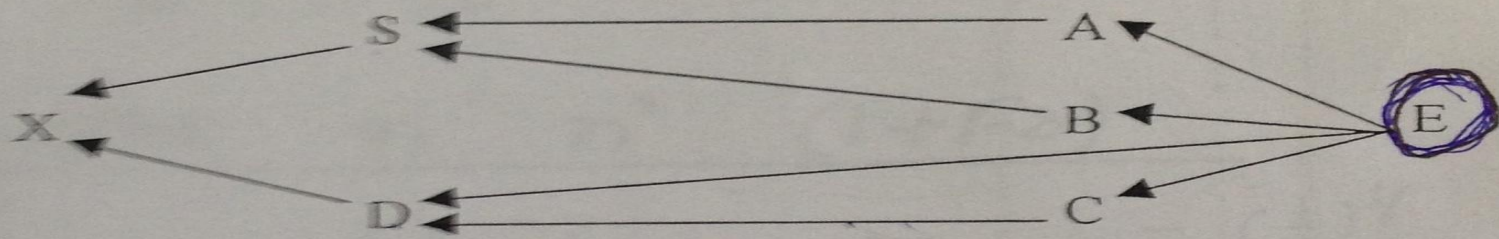
Also calculate R_{XE} for this pedigree.

F_X, R_{XE}

$$R_{SD} = \frac{0.375}{\sqrt{(1+0.125)(1+0.25)}}$$
$$= \frac{0.375}{\sqrt{(1.125)(1.25)}} = \frac{0.375}{1.186} = 0.3162 = 31.62\%$$

Relationship and inbreeding coefficients

(B)



Also calculate R_{XE} for this pedigree.

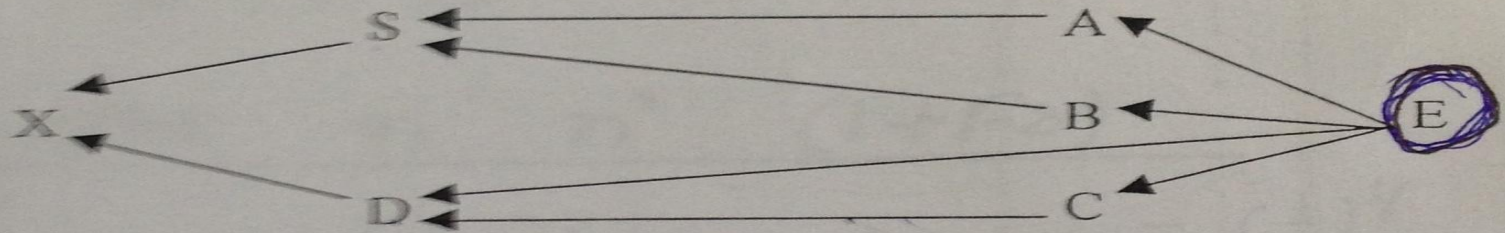
F_X, R_{XE}

R_{XE}	ancestor	n	n'	$(1+F_0)$	
$\rightarrow X$	E	0	3	—	$= (\frac{1}{2})^3$
$\rightarrow X$	E	0	3	—	$= (\frac{1}{2})^3$
$\rightarrow X$	E	0	2	—	$= (\frac{1}{2})^2$
$\rightarrow X$	E	0	3	—	$= (\frac{1}{2})^3$

$$\begin{aligned}
 R_{XE} &= (\frac{1}{2})^3 + (\frac{1}{2})^3 + (\frac{1}{2})^2 + (\frac{1}{2})^3 \\
 &= 0.125 + 0.125 + 0.25 + 0.125 \\
 &= 0.625
 \end{aligned}$$

Relationship and inbreeding coefficients

(B)



Also calculate R_{XE} for this pedigree.

F_X, R_{XE}

$$R_{XE} = \frac{0.625}{\sqrt{(1+0)(1+0.1875)}}$$
$$= \frac{0.625}{\sqrt{1.1875}} = \frac{0.625}{1.0897} = 0.5736$$
$$= 57.36\%$$

Thanks for your attention